

**University
of Basel**

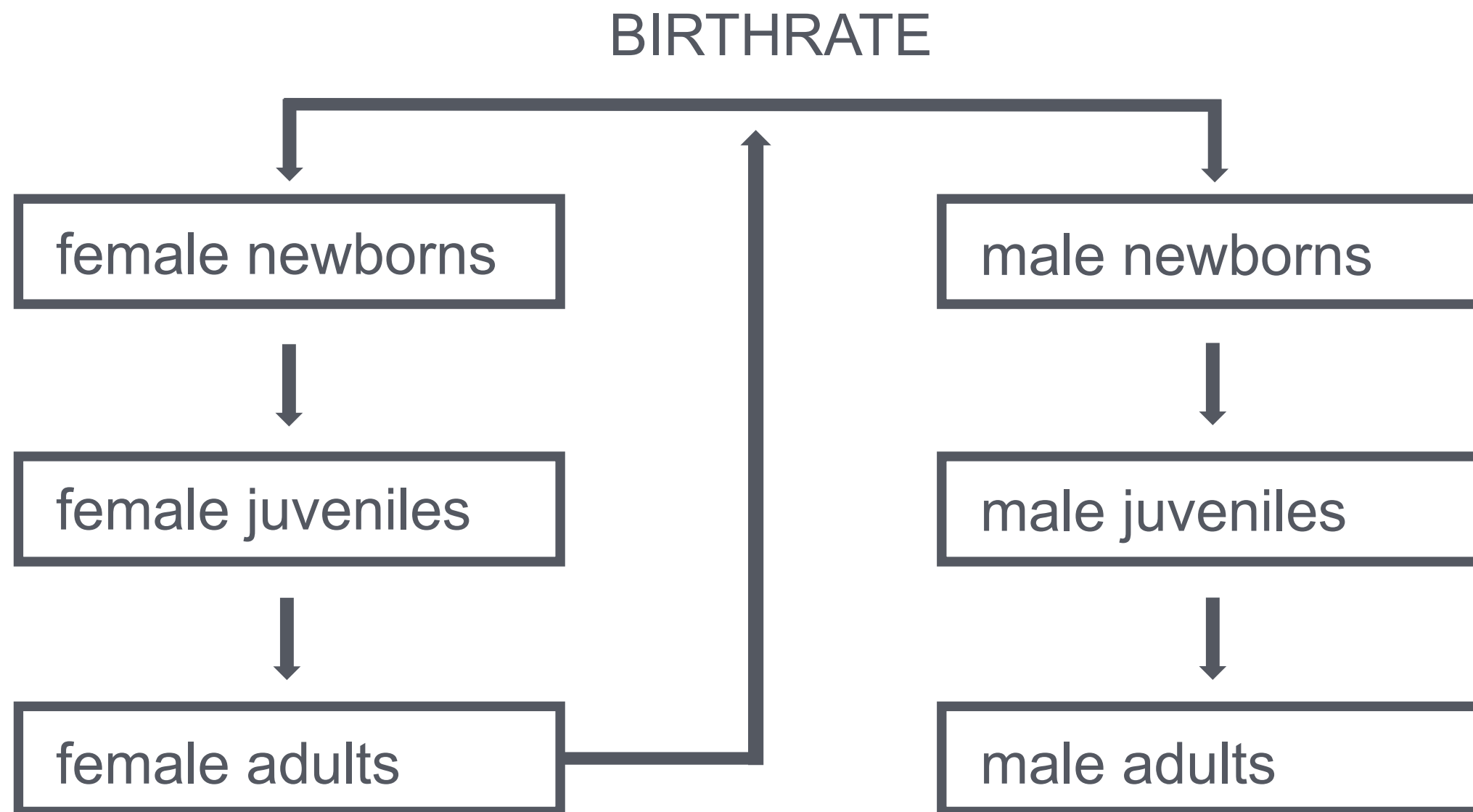
In association with:



Swiss Tropical and Public Health Institute
Schweizerisches Tropen- und Public Health-Institut
Institut Tropical et de Santé Publique Suisse

Solving the formula (part one)

Schematic representation of a demographic model of an animal population



N =
young / calves
subadult / heifers
adult / cows

$$\left(\begin{array}{c} N = \\ Y \\ S \\ A \end{array} \right)$$

$$\mathbf{P} = \begin{matrix} 0 & 0 & \text{birth rate} \\ \text{survival young} & \text{persistence subadult} & 0 \\ 0 & \text{survival subadult} & \text{persistence adult} \end{matrix} \left(\mathbf{P} = \begin{pmatrix} 0 & 0 & b \\ sy & ps & 0 \\ 0 & ss & pa \end{pmatrix} \right)$$

$$\mathbf{N}_{t+1} = \mathbf{P}^n \times \mathbf{N}_t$$

$$\begin{array}{ccc}
 & \downarrow & \downarrow \\
 \mathbf{P} = \begin{pmatrix} 0 & 0 & b \\ sy & ps & 0 \\ 0 & ss & pa \end{pmatrix} & \times & \mathbf{N} = \begin{pmatrix} Y \\ S \\ A \end{pmatrix}
 \end{array}$$

$$\mathbf{N}_{t+1} = \mathbf{P}^n \times \mathbf{N}_t$$

Result after 20 – 30 iterations

$$\mathbf{P}^n = \begin{pmatrix} \lambda^n & 0 & 0 \\ 0 & \lambda^n & 0 \\ 0 & 0 & \lambda^n \end{pmatrix}$$

$$\mathbf{P}^n = \lambda^n$$

$$Y = 50'000$$

$$S = 20'000$$

$$A = 40'000$$

$$b = 60\% = 0.6$$

$$sy = 70\% = 0.7$$

$$ps = 50\% = 0.5$$

$$ss = 60\% = 0.6$$

$$pa = 65\% = 0.65$$

$$\begin{pmatrix} 0 & 0 & b \\ sy & ps & 0 \\ 0 & ss & pa \end{pmatrix} \times \begin{pmatrix} Y \\ S \\ A \end{pmatrix} \Rightarrow \begin{matrix} (0 \times Y) + (0 \times S) + (b \times A) \\ (sy \times Y) + (ps \times S) + (0 \times A) \\ (0 \times Y) + (ss \times S) + (pa \times A) \end{matrix}$$

↓

$$\begin{pmatrix} 0 & 0 & 0.6 \\ 0.7 & 0.5 & 0 \\ 0 & 0.6 & 0.65 \end{pmatrix} \times \begin{pmatrix} 50'000 \\ 20'000 \\ 40'000 \end{pmatrix} \Rightarrow \begin{matrix} 0.6 \times 40'000 = \mathbf{24'000} \\ (0.7 \times 50'000) + (0.5 \times 20'000) = \mathbf{45'000} \\ (0.6 \times 20'000) + (0.65 \times 40'000) = \mathbf{38'000} \end{matrix}$$